# **Procedural Cloudscapes (supplementary material)**

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## 1. General precisions

We use a combination of scaled cellular noise, or Worley noise, and gradient noise functions which in our implementation defaults to Simplex noise.

For clarity, we define the following:

- $G_3(o, p, l, f, \mathbf{p}) \in [0, 1]$ , a sum of *o* octaves of 3D gradient noises defined with persistence *p* and lacunarity *l*, with a base frequency *f*, evaluated at a position  $\mathbf{p} = (x, y, z)$ . Similarly, we define  $G_2$  as a sum of 2D gradient noises over position (x, y).
- W<sub>3</sub>(o, p, l, f, p) ∈ [0, 1]. W<sub>3</sub> is a sum of o octaves of complemented 3D Worley noise, likewise defined with persistence p, lacunarity l and frequency f. Each octave is defined as 1 − w, where w is a classic Worley noise in the range [0, 1].

• 
$$H(a,b,t) = \begin{cases} 0 & \text{if } t < a \\ 1 & \text{if } t > b \\ u^2(3-2u) & \text{otherwise, with } u = \frac{t-a}{b-a} \end{cases}$$

*H* yields a value in [0,1] and performs a smooth Hermite interpolation between *a* and *b*.

• Finally, we define the scale of the scene: one modeling unit corresponds to a hundred meters.

## where

$k_2 = (1 - k_1) + k_1 n_5$	(3)
$k_{1} = H(0 \mid 0 \mid 0 \mid n_{1})^{2}$	(4)

$$k_1 = H(0.1, 0.9, n_4)^2$$
(4)
$$\mathbf{p}_n = (x_n, y_n, z_n) = \mathbf{p}/1080$$
(5)

$$n_2 = G_3(8, 0.52, 2.02, 15, (0.65x_n, y_n, z_n) + \mathbf{q}_2)$$
(6)

$$n_6 = W_3(4, 0.33, 3, 160, \mathbf{p}_n + \mathbf{q}_6)$$
(10)

$$n_7 = W_3(2, 0.5, 2, 240, \mathbf{p}_n + \mathbf{q}_7)$$
(11)

$$\mathbf{p}_8 = G_3(8, 0.52, 2.02, 288, \mathbf{p}_n + \mathbf{q}_8)$$
(12)  
$$\mathbf{p}_8 = G_8(8, 0.52, 2.02, 384, \mathbf{p}_n + \mathbf{q}_8)$$
(13)

$$\mathbf{a}_{2} = (-\tau, 0, 0) \tag{13}$$

$$\mathbf{q}_2 = (-\tau, 0, 0) \tag{14}$$

$$\mathbf{q}_{6} = (-4\tau, 0, 0) \tag{16}$$

$$\mathbf{q}_7 = (-0.8\tau, 0, 0)$$
 (17)

$$\mathbf{q}_8 = (-8\tau, 0, 0)$$
 (18)

$$\mathbf{q}_9 = (-8\tau, 0, 0) \tag{19}$$

 $\tau$  is the time offset added for animating the clouds, unit being hours. Notice that the offset works along the *x* axis, so prior to evaluating  $\phi$  and  $\delta$  one should change the frame of reference for position **p** to match the local direction of the wind.

### 2. Cumulus

#### 3. Altostratus and Altocumulus

$$\phi = 2k_2 n_3 H(0.45, 0.65, n_2) \tag{1}$$

$$\delta = 0.77((1 - n_6) + 0.5(1 - n_7) + 0.25n_8 + 0.5n_9)$$
(2)

 $\phi = k + (1 - k)H(0.43, 1, n_1) \tag{20}$ 

$$\delta = (1 - k)(0.75n_2 + 0.25(1 - n_3)) \tag{21}$$

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where

$$\begin{aligned} \mathbf{p}_n &= (x_n, y_n, z_n) = \mathbf{p}/1080 & (22) \\ n_1 &= G_3(8, 0.52, 2.02, 36, (0.35x_n, y_n, z_n) + \mathbf{q}_1) & (23) \\ n_2 &= G_3(8, 0.52, 2.02, 96, \mathbf{p}_n + \mathbf{q}_2) & (24) \\ n_3 &= W_3(4, 0.33, 3, 400, \mathbf{p}_n + \mathbf{q}_3) & (25) \\ \mathbf{q}_1 &= (-2\tau, 0, 0) & (26) \\ \mathbf{q}_2 &= (-8\tau, 0, 0) & (27) \end{aligned}$$

$$\mathbf{q}_3 = (-8\tau, 0, 0)$$
 (28)

 $k \in [0, 1]$  is a morphing parameter between the closely related *Altostratus* and *Altocumulus*, as the two types co-occur under the same meteorological conditions. For pure *Altostratus* k = 1, for pure *Altocumulus* k = 0 and any value in between gives a continuous blend between the two types. Here  $\tau$  follows the same definition as shown above for *Cumulus*.